

# Origin of photoluminescence in tetrahedrally-bonded amorphous semiconductors and amorphous chalcogenides\*

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Using wideband quadrature frequency resolved spectroscopy (QFRS) expanded for lifetime measurement from 2 ns to 160 s, we have revealed that the lifetime distribution of the photoluminescence (PL) of a-Si:H is a triple-peak structure having the third peak at a lifetime  $\geq 0.1$  s, instead of the well-known double peaks at  $\sim\mu\text{s}$  and  $\sim\text{ms}$ . Moreover, the triple-peak phenomenon has been found to occur universally among non-crystalline semiconductors such as a-Ge:H and a-SiN:H, and chalcogenide glasses. The dependences of the QFRS spectra on temperature, excitation intensity and energy, emission energy and magnetic fields have elucidated that both *geminat*e or *excitonic* recombination and *non-geminat*e, or *distant pair* (DP) recombination co-exist in PL of non-crystalline semiconductors, which has settled the controversy as to whether the recombination is *germinate* or *non-germinate* in the PL. Observing the residual PL decay together with the QFRS in a-Si:H, we have also resolved the long-standing disagreement between the PL and light-induced electron spin resonance (LESR) signal. In addition, the paper presents the different effects of electric field on the two types of recombination.

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## 1. Introduction

Research on recombination of photoexcited carriers in non-crystalline semiconductors is important for their application to optoelectronic devices such as solar-cells, light sensors and light emitters. Since photoluminescence (PL) is caused by radiative recombination of the photoexcited carriers, PL spectroscopy is a popular, relatively simple and well-established tool for studying the recombination mechanisms. In addition to conventional measurements of the PL spectrum, measurement of the PL lifetime distribution provides us with important insights to reveal the recombination mechanisms. Quadrature frequency resolved spectroscopy (QFRS) of PL is effective in analysing the lifetime distribution at sufficiently low generation rates of photocarriers  $G$ , in contrast to time resolved spectroscopy (TRS) [1].

High-quality films of hydrogenated tetrahedrally-bonded amorphous Si (a-Si:H) are one of the rather easily obtainable and important materials for optoelectronics applications. A salient feature of a-Si:H is the existence of

an intrinsic distribution of band-tail localized states, which strongly influence the electronic and optical properties.

The two types of recombination of an electron-hole (e-h) pair can be considered in the PL of a-Si:H, as well as other amorphous semiconductors at low temperatures,  $T$ . One is *geminat*e recombination, where an e-h pair is created by a photon of energy exceeding the band-gap and mutually coupled by a Coulomb attractive force. In *geminat*e recombination, the Coulombic effect allows the pair to recombine within itself. In particular, a *geminat*e e-h pair having a hydrogen-like system is called an *exciton*, which is classified into two electronic states; *singlet* ( $S = 0$ ) and *triplet* ( $S = 1$ ) according to the total spin  $S$  of the e-h pair.

The other is *non-geminat*e, or *distant-pair* (DP) recombination, where an electron escapes from its partner hole of an e-h pair created by the identical photon and can recombine with a hole created by another photon. While e-h pairs with energies exceeding the band edges for band-to-band excitation relax to the band edges via thermalization and hop down into the band-tail localized states, some of them split into electrons and holes, which randomly distribute themselves in the localized states. The

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DP recombination occurs preferentially for a pair with the shorter e-h distance  $r$  with a recombination lifetime  $\tau$  given by the radiative tunnelling (RT) model at low  $T$ ,

$$\tau = \tau_o \exp(2r/a) \quad (1)$$

where  $\tau_o$  is radiative electric dipole transition time of the order of 1 ~ 10 ns and  $a$  is the larger extent of either the electron or hole wave-function, being a localized electron radius of ~1 nm in the case of a-Si:H [2].

Exciton involvement in the PL of a-Si:H at low temperatures was once suggested [3,4]. Probably owing to the disorder of amorphous materials in contrast to crystalline ones, however, excitonic absorption spectrum has not been observed except for a-SiO<sub>2</sub>. Therefore, the PL in a-Si:H, whether it is geminate or non-geminate, has been often interpreted in terms of the RT model [2]. In contrast, the PL of a-As<sub>2</sub>S<sub>3</sub> and a-As<sub>2</sub>Se<sub>3</sub> has been frequently interpreted in terms of the exciton model. Thus, in a-Si:H, the main emphasis has been placed for a long time rather on a controversy as to whether the PL originates from geminate or non-geminate (DP) recombination.

Using QFRS to measure the PL lifetime distributions, Bort *et al.* [5] discovered a geminate condition at the generation rate  $G \approx 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$  in a-Si:H, below which the peak lifetime  $\tau_T$  (~ms) is independent of  $G$  and thus the metastable or steady-state photocarrier density  $n_T = G\tau_T$  is *proportional* to  $G$ . Above the geminate condition  $G > 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$ ,  $\tau_T$  decreases with increasing  $G$ , which is interpreted by the DP recombination with the RT model. Hence the sub-linear dependence of  $n_T = G\tau_T$  on  $G$  is predicted at  $G > 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$ .

However, the intensity of the light-induced electron spin-resonance (LESR), analogous to  $n_T$ , is known to be sub-linearly dependent on  $G$  approximately as  $\propto G^{0.2}$  in the whole range of  $G$  from  $10^{13}$  to  $10^{23} \text{ cm}^{-3} \text{ s}^{-1}$  [5-7]. The DP recombination model successfully predicts this sub-linear  $G$ -dependence of the LESR intensity, but it fails to explain the linear dependence of  $n_T$  on  $G$  below the geminate condition, where the lifetime  $\tau_T$  is constant [8].

It has been already established by QFRS that the PL lifetime distribution is double-peaked in a-Si:H, consisting of short-lived (~ $\mu$ s) and long-lived (~ms) components under the geminate condition. However it is difficult to identify the two lifetime components on the basis of the RT model [9,10]. Stachowitz *et al.* [11] proposed exciton involvement in the double peak phenomena, attributing the short- and long-lived components to a singlet ( $S = 0$ ) exciton and triplet ( $S = 1$ ) exciton, respectively.

Developing the wideband QFRS technique which allows analysis of lifetimes over almost 11 decades from 2 ns to 160 s, we observed double-peak lifetime behaviour in not only tetrahedrally-bonded a-Ge:H and a-SiN:H but also amorphous chalcogenides, e.g. g-As<sub>2</sub>S<sub>3</sub> and a-Se, and supported the exciton model [12-14].

The wideband QFRS also revealed that the lifetime distribution is triple-peaked, accompanied by a third lifetime peak in the long lifetime range of 0.1 ~ 160 s in

the PL of a-Si:H and a-Ge:H under the geminate condition. The third component exhibited characteristic features of the DP recombination [15]. Thus, we claimed that *geminate recombination* and *non-geminate (DP) recombination co-exist* in the PL of a-Si:H and a-Ge:H even under the geminate condition at low  $T$  and low  $G$ . Moreover, a similar phenomenon was observed in chalcogenide amorphous semiconductors, indicating that the triple-peak QFRS spectrum, i.e., the *co-existence of geminate and non-geminate recombination*, is universal among amorphous semiconductors [16-18].

Moreover, PL recombination for lifetimes longer than 160 s was investigated by observing the residual PL decay after cessation of PL excitation in a-Si:H at low  $G$  [19]. This very long-lasting PL decay, as well as the DP component of QFRS spectra, resolves the long-standing controversy concerned with the  $G$ -dependences of the steady-state photo-generated carrier density in the PL and the LESR intensity [15,19,20].

The present paper reviews our previously published results, demonstrating both excitonic recombination and DP recombination in PL of undoped a-Si:H and other amorphous semiconductors. We also claim that the residual PL decay persisting for more than  $\sim 10^4$  s reflects the decay kinetics of the DP recombination and consistency with the LESR results. The paper also presents the difference of the electric-field effect on the PL between the geminate or excitonic recombination and the DP recombination in a-Si:H [21,22].

## 2. Coexistence of geminate recombination and non-geminate recombination

### 2.1 Triple-peak lifetime distribution

Fig. 1 shows QFRS spectra of a-Si:H from 2 ns to 160 s excited at the PL excitation energy  $E_X = 2.33$  eV for various generation rates  $G$ , from  $2.5 \times 10^{15}$  to  $5.0 \times 10^{22} \text{ cm}^{-3} \text{ s}^{-1}$  [20]. We can see that the long- and short-lived components are fixed at  $\tau_T \approx 4$  ms and at  $\tau_S \approx 2$   $\mu$ s, respectively, even though  $G$  changes from  $2.5 \times 10^{15}$  to  $4.1 \times 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$ . This is the well-known double-peak lifetime distribution observed under the so-called geminate condition  $G \leq 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$  [9,10].

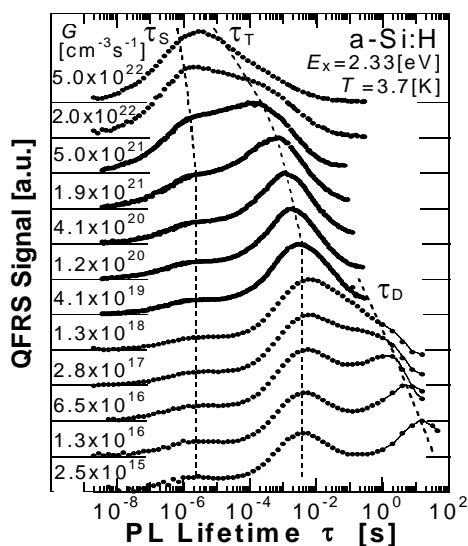


Fig. 1 QFRS spectra from 2 ns to 160 s for a-Si:H at 3.7 K and  $E_x = 2.33$  eV with various  $G$  [20].

However, a new third peak higher than the other two is observed at  $\tau_D \approx 20$  s for  $G \approx 2.5 \times 10^{15} \text{ cm}^{-3} \text{ s}^{-1}$ , which might have been overlooked earlier due to the lack of the very low frequency QFRS.

As  $G$  increases,  $\tau_D$  continuously shifts to shorter lifetimes and the peak merges with the  $\tau_T$  component at  $G \approx 1.3 \times 10^{18} \text{ cm}^{-3} \text{ s}^{-1}$ . The continuous shortening of  $\tau_D$  with increasing  $G$  is a distinctive feature of the DP recombination based on Eq. (1) of the RT model and the plot of  $\tau_D$  vs.  $G$  fits well the curve calculated from the balance equation [23]. Thus, the PL lifetime distribution of an intrinsic a-Si:H is triple-peaked at a low  $T$  of 3.7 K under the geminate condition  $G \leq 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$ . At sufficiently low  $G$ , the three peaks possess well-separated

lifetimes, suggesting that the recombination events at  $\tau_S$ ,  $\tau_T$  and  $\tau_D$  occur via three independent, or non-competing recombination channels.

Similar triple-peaked lifetime structures are also observed in the  $G$ -dependent QFRS spectra of a-Ge:H excited at  $E_x = 1.81$  eV and  $T = 3.7$  K under the geminate condition  $G \leq 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$  [15]. We have also observed the DP component in a-SiN:H [13] and chalcogenides such as g-As<sub>2</sub>S<sub>3</sub>, a-As<sub>2</sub>Se<sub>3</sub>, a-Se and g-GeGaSe [16-18], as well as the double-peaks at  $\tau_S$  and  $\tau_T$  except for a-As<sub>2</sub>Se<sub>3</sub> [14, 24]. However, the DP component is less pronounced and its dependence on  $G$  is rather indistinguishable in these amorphous semiconductors, which is due to the competing non-radiative recombination via defects [13].

Fig. 2(a) demonstrates the triple-peaked QFRS spectra of GeGaSe chalcogenide glass for various emitted photon energies  $\hbar\omega$ , showing the triple peaks at  $\tau_S$ ,  $\tau_T$  and  $\tau_H$ . The third peak located at a lifetime  $\tau_H \approx 20$  s arises from the DP recombination, which is strongly influenced by the non-radiative recombination via defects, exhibiting a very weak dependence of  $\tau_H$  on  $G$  and  $E_x$  [17,18].

Fig. 2(b) demonstrates the quantum efficiencies (QEs)  $\eta_S$ ,  $\eta_T$  and  $\eta_H$  corresponding to the  $\tau_S$ -,  $\tau_T$ - and  $\tau_H$ -components obtained by deconvoluting the QFRS spectra (a) as functions of  $\hbar\omega$ , i.e., the PL spectra of the individual recombination events. The peak energy of the  $\tau_S$ -component  $\sim 1.02$  eV is higher by  $\sim 80$  meV than that of the  $\tau_T$ -component  $\sim 0.94$  eV. This suggests that the exchange energy  $E_{ex}$  between the singlet exciton ( $\tau_S$ -component) and the triplet exciton ( $\tau_T$ -component) is  $\sim 80$  meV, in contrast to  $E_{ex} \approx 40$  meV for a-Si:H [25].

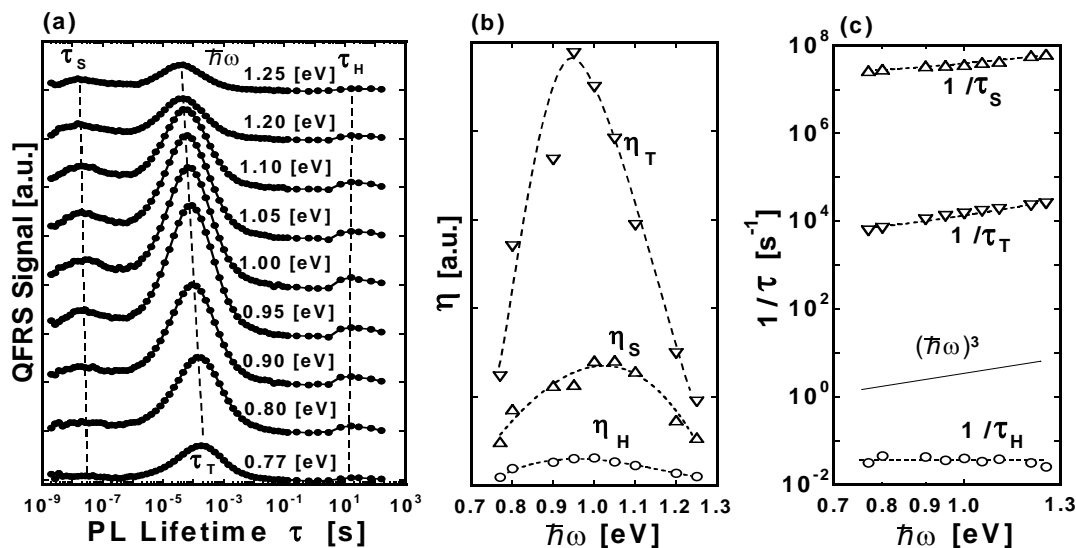


Fig.2 (a) PL emission energy  $\hbar\omega$ -evolved QFRS spectra of undoped g-GeGaSe at  $E_X = 2.33$  eV,  $T = 3.7$  K and  $G \approx 10^{20}$  cm<sup>-3</sup>s<sup>-1</sup>. (b) The three components of  $(\Delta)$   $\eta_S$ ,  $(\nabla)$   $\eta_T$ ,  $(\circ)$   $\eta_H$  deconvoluted from (a) as functions of  $\hbar\omega$ , i.e., the PL spectra of QEs  $\eta_S, \eta_T$  and  $\eta_H$ . (c) Radiative recombination rates  $(\Delta)$   $1/\eta_S$ ,  $(\nabla)$   $1/\eta_T$  and  $(\circ)$   $1/\eta_H$  of the three components plotted against  $\hbar\omega$  on a log-log scale [18].

Fig. 2(c) shows the recombination rate  $\tau^{-1}$  of each component as a function of  $\hbar\omega$  on a log-log scale. The recombination rates  $\tau_S^{-1}$  and  $\tau_T^{-1}$  roughly depend on  $\hbar\omega$  as  $\propto (\hbar\omega)^3$ , which supports that the  $\tau_S$ - and  $\tau_T$ -components are ascribed to the excitonic recombination process as those of a-Si:H [19,25]. On the other hand, the recombination rate  $\tau_H^{-1}$  is almost independent of  $\hbar\omega$ . This suggests that the  $\tau_H$  component should be ascribed to the DP recombination of photoexcited carriers after hopping down in band-tail states [16-19].

## 2.2 Excitonic recombination

The singlet exciton lifetime  $\tau_S$ , the triplet exciton lifetime  $\tau_T$  and the spin-exchange energy  $E_{ex}$  obtained by QFRS are tabulated for various amorphous semiconductors in Table 1. We can see that  $\tau_S$  widely ranges from 10 ns, being close to the

Table 1. Singlet ( $\tau_S$ ) and triplet ( $\tau_T$ ) exciton lifetimes and spin-exchange energy ( $E_{ex}$ ) for various amorphous semiconductors.

	$\tau_S$ ( $\mu$ s)	$\tau_T$ (ms)	$E_{ex}$ (meV)
a-Si:H	2	4	40
a-Ge:H	20	0.8	—
a-SiN:H	0.01	1	50 ~180
g-As <sub>2</sub> S <sub>3</sub>	0.01	0.1	100
a-As <sub>2</sub> Se <sub>3</sub>	—	0.8	—
a-Se	0.2	1	160
g-GeGaSe	0.02	0.1	80

electric-dipole transition time  $\tau_0$ , to 20  $\mu$ s for the various materials. This can be explained by invoking self-trapped excitons (STEs), as follows [24-27].

After excitation of an e-h pair in a-Si:H, a hole of the pair will be immediately self-trapped as the self-trapped hole (STH) with a radius  $a_h$  in a deeply-localized state of the valence-band-tail having a higher density of states, while its partner electron is rather free owing to the lower density of conduction-band-tail states. The electron will be loosely-bound to the STH by Coulomb attraction, forming a STE rather than trapped to a localized state of the conduction-band-tail. Thus the STE has a Bohr radius  $a_B^*$  larger than the electron localization radius in the conduction-band-tail  $a$  usually  $\sim 1$  nm for a-Si:H. The discrepancy in the orbital size between the initial state ( $a_B^*$ ) and the final state ( $a_h$ ) reduces the radiative transition rate of the singlet STE by an amount  $(a_h/a_B^*)^3$  [24-26].

Furthermore, the formation of the three lifetime components in amorphous chalcogenides has been interpreted on the basis of the Mott-Davis-Street (MDS) model [17,18,28].

Kivelson and Gelatt [27] gave the radiative transition rate  $\tau_S^{-1}$  of the singlet exciton as

$$\frac{1}{\tau_S} = \frac{4}{3} \kappa^{1/2} \left[ \frac{e^2}{\hbar c} \right] \left[ \frac{\omega^3}{c^2} \right] a_h^2 S, \quad (2)$$

where  $\kappa$  is the static dielectric constant,  $e^2/(\hbar c) \approx 1/137$  is the fine structure constant,  $\hbar\omega$  is the emitted photon energy,  $c$  is the speed of light, and  $S$  is an overlap term given by  $\sim (2a_h)^3/(a_B^*)^3$ . If  $S$  is omitted from the right-hand side of Eq. (2), it is equal to the radiative electric-dipole transition rate  $\tau_0^{-1}$  with an electric-dipole moment  $ea_h$  given by Wilson *et al.* [29]. Since  $a_B^*$  for a-Si:H was estimated to be  $\sim 2.4$  nm by Kivelson and Gelatt [27] and  $\sim 5$  nm by us [20] as described in Section 2.3, we obtain  $\tau_S$  ranging from  $\sim 1.2$  to  $\sim 11$   $\mu$ s, with the photon energy  $\hbar\omega = 1.5$  eV,  $\kappa = 12$  and  $a_h = 0.2$  nm. As Eq. (2) has an order of magnitude uncertainty, our experimental result of  $\tau_S \approx 2$   $\mu$ s agrees quite satisfactorily with the estimated values. Lifetimes of the singlet and triplet excitons are calculated for amorphous semiconductors using different recombination models from that mentioned in Section 2.3 [30,31].

Wilson *et al.* observed  $\tau_S \approx 10$  ns for a-Si:H by TRS [29]. As far as the author knows, however, there is no TRS of PL in a-Si:H under the geminate condition except for that of Stearns [32], where the PL decay  $I(t)$  was non-exponential in the range of time  $t = 0.5 \sim 40$  ns after PL excitation. The plot of  $t \times I(t)$  as a function of  $\log t$  gives an approximate lifetime distribution similar to the QFRS spectrum [1]. We show the QFRS spectrum of PL in a-Si:H at  $\hbar\omega \approx 1.5$  eV and superimpose the plot of  $t \times I(t)$  obtained from the Stearns' data in Fig. 3. This also proves the absence of a peak in the ns region of the TRS in the PL of a-Si:H under the geminate condition [24].

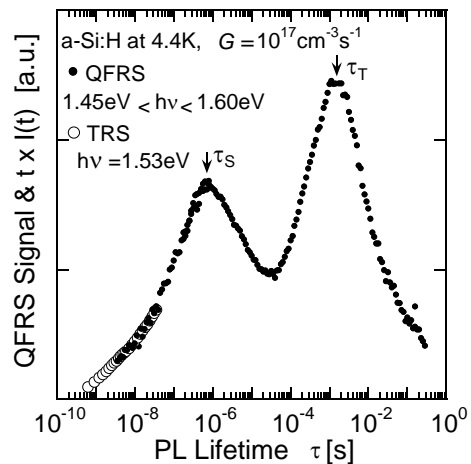


Fig. 3 (●) QFRS spectrum of PL with emission energy  $1.45 < h\nu < 1.60$  eV for a-Si:H under the geminate recombination condition  $G \approx 10^{17}$  cm<sup>-3</sup>s<sup>-1</sup> at 4.4 K and  $E_X = 2.33$  eV. (○) Plots of  $t \times I(t)$  vs.  $\log_{10} t$  obtained from Stearns' TRS data [24,32].

### 2.3 Steady-state photocarrier density of geminate and non-geminate recombination

Deconvoluting the QFRS spectra for various  $G$  in Fig. 1, we obtain the steady-state or metastable photocarrier densities of the three recombination components of PL in a-Si:H, i.e.,  $n_S = \eta_S G \tau_S$  (□),  $n_T = \eta_T G \tau_T$  (▲) and  $n_D = \eta_D G \tau_D$  (○) as functions of  $G$  as shown in Fig. 4. It is a characteristic feature of geminate or excitonic recombination that the steady-state carrier densities  $n_S$  and  $n_T$  increase linearly against  $G$ , while the lifetimes  $\tau_S$  and  $\tau_T$  remain constant. On the other hand, with increasing  $G$ ,  $\tau_D$  decreases and thus  $n_D = \eta_D G \tau_D$  increases sub-linearly with  $G$ , roughly as  $n_D \propto G^{0.2}$ .

The LESR spin density vs.  $G$  (Δ, ∇, ●) obtained by other three groups is also plotted in Fig.4, which agrees with  $n_D$  vs.  $G$  (○) without any adjusting parameters [5,7]. This suggests that the LESR results reflect the DP recombination, which is discussed in more detail in Section 3.

The steady-state carrier concentration  $n_T$  of the  $\tau_T$ -component increases almost in proportion to the generation rate  $G$  under the geminate condition  $G \leq 10^{19}$  cm<sup>-3</sup>s<sup>-1</sup> as reported in [5]. When  $G$  exceeds  $10^{19}$  cm<sup>-3</sup>s<sup>-1</sup>, the plot of  $n_T$  merges with the sub-linear plot of  $n_D \propto G^{0.2}$  at the steady-state carrier density  $n_T \approx n_D \approx 10^{17}$  cm<sup>-3</sup>. At  $G \approx 10^{19}$  cm<sup>-3</sup>s<sup>-1</sup>, the triplet exciton component and the DP component can be seen merging in the QFRS spectra (Fig. 1). This implies that the recombination of the triplet exciton is prevailed over by that of DP at  $n_T \approx 10^{17}$  cm<sup>-3</sup>.

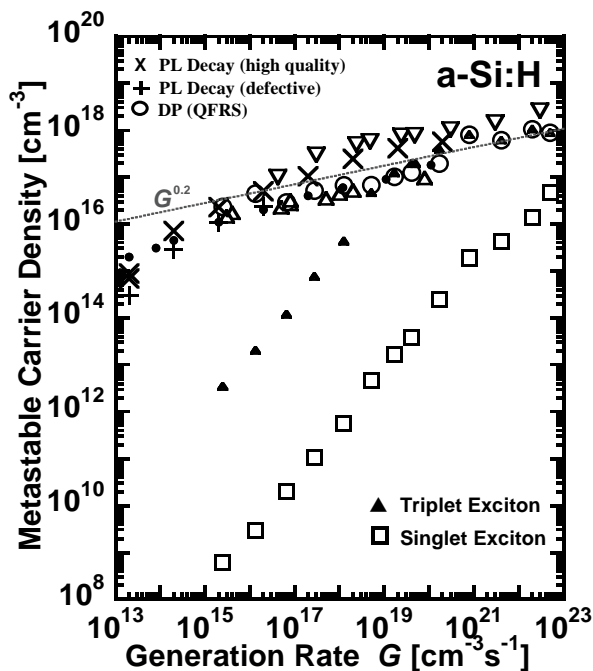


Fig. 4 Metastable carrier density  $n_{met}$  vs. generation rate  $G$ ; × and + denote  $n_{met}$  deduced by integrating the PL decay for a high-quality film and a defective film of a-Si:H, respectively. The plots ○, □ and ▲ indicate the steady-state carrier densities  $n_D$ ,  $n_S$  and  $n_T$ , respectively, obtained from the QFRS spectra in Fig.1., and ● denote the LESR densities obtained from [5], [6] and [7], respectively. The unit of the plots of  $n_{met}$  is arbitrary [6]. The straight line indicates  $n_{met} \propto G^{0.2}$ .

Similarly, an extrapolation of the plot of  $n_S$  vs.  $G$  intersects with the sub-linear plots at around  $n_S \approx n_D \approx 10^{18}$  cm<sup>-3</sup> ( $G \approx 10^{23} \sim 10^{24}$  cm<sup>-3</sup>s<sup>-1</sup>), though it deviates from a straight line above  $G \approx 10^{21}$  cm<sup>-3</sup>s<sup>-1</sup> owing to the irradiation condensed by a lens. Such a coalescence of all the components is also seen at  $G \approx 5.0 \times 10^{22}$  cm<sup>-3</sup>s<sup>-1</sup> in Fig. 1.

If the triplet excitons are assumed to be transformed to DPs at the point of coalescence with  $n_T \approx n_D$ , the average e-h distance of the DPs given by  $\sim 0.5n_T^{-1/3}$  is estimated to be  $\sim 10$  nm by  $n_T \approx n_D \approx 10^{17}$  cm<sup>-3</sup>. This suggests that the Bohr radius of the triplet excitons is close to  $\sim 10$  nm. Similarly, at the coalescence of the singlet excitons and DPs at around  $n_S \approx n_D \approx 10^{18}$  cm<sup>-3</sup> the average e-h distance  $\sim 0.5n_S^{-1/3}$  amounts to  $\sim 5$  nm [20]. Thus a singlet exciton radius  $a_B^*$  is considered to be close to  $\sim 5$  nm and then the exciton binding energy  $e^2/2\kappa a_B^*$  works out to be  $\sim 5$  meV with a dielectric constant  $\kappa \approx 12$ , which explains the disappearance of the  $\tau_S$ -component at low  $T \approx 30$  K [20].

Fig. 5 illustrates a model of PL in a-Si:H composed of three lifetime components, i.e., a singlet exciton ( $\tau_S$ ), a triplet exciton ( $\tau_T$ ) and a DP ( $\tau_D$ ) [1,13]. It should be noted that the excitonic recombination model shown here is different from the previous one [33]. The larger exchange energy  $E_{ex} \approx 40$  meV than the binding energy of singlet exciton is probably attributable to localization of STEs [1,20].

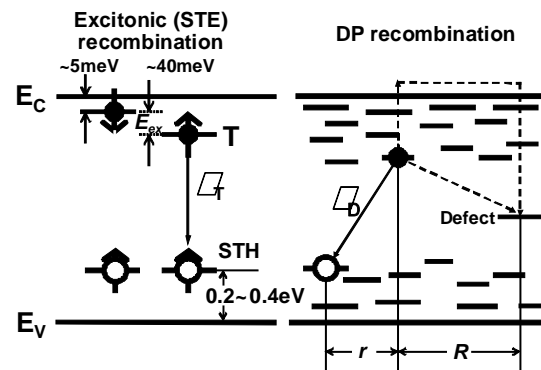


Fig.5 Recombination model of a-Si:H consisting of

singlet ( $\tau_s$ ) and triplet ( $\tau_t$ ) self-trapped excitons (STE) and distant-pairs (DP( $\tau_D$ )) with  $e$ - $h$  pair separation  $r$ . The exchange energy  $E_{ex} \approx 40$  meV and singlet-exciton binding energy  $\sim 5$  meV are obtained in [25] and [20] respectively. The electron of the DP has a distance  $R$  to a defect. Thin solid arrows indicate radiative recombination. An oblique dotted arrow indicates non-radiative tunnelling and vertical one to the defect indicates non-competing non-radiative recombination. Thick arrows indicate spins of electrons and holes [13].

The PL model of amorphous chalcogenides is given on the basis of the MDS model in our previous papers [17,18].

### 3. Consistency between metastable PL carrier density and LESR intensity.

Fig. 6 shows log-log plots of PL intensity  $I(t)$  vs. time  $t$  after cessation of PL excitation of 2.33 eV, i.e.,  $\log_{10}I(t)$  vs.  $\log_{10}t$  for various values of  $G$  from  $10^{13}$  to  $10^{19}$   $\text{cm}^{-3}\text{s}^{-1}$  taken for a-Si:H at 3.7 K. Except for the lowest  $G$  value of  $2 \times 10^{13}$   $\text{cm}^{-3}\text{s}^{-1}$ , the PL decay curves converge asymptotically at long times of  $\sim 10^4$  s, even though they are initially different by 5 orders of magnitude. Since excitonic or geminate recombination affects the early stage of

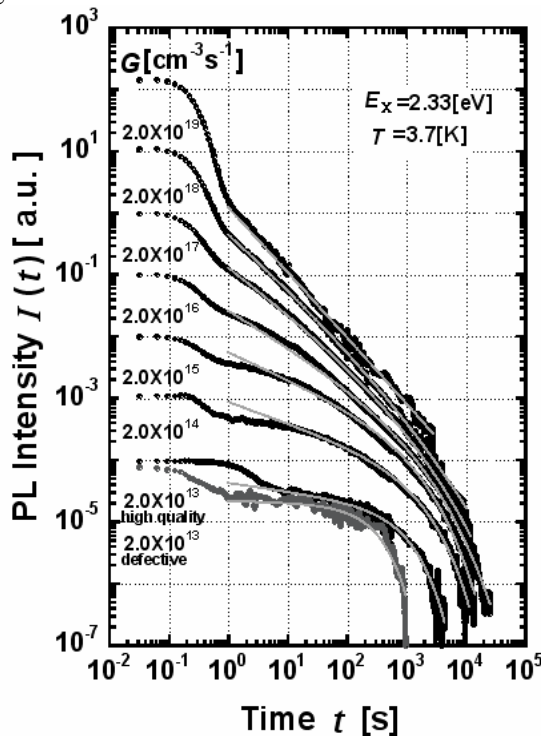


Fig. 6. Log-log plots of PL decay  $I(t)$  of a high-quality a-Si:H film with various values of  $G$  at 3.7K. The plots are fitted to the derivative of the SE functions (half-tone curves). The plots in half-tone are for a defective film at  $G = 2 \times 10^{13}$   $\text{cm}^{-3}\text{s}^{-1}$  [19].

the PL decay at times  $t < 1$  s, we have fitted each curve, at times long enough after switching off the PL excitation, to the derivative of a stretched exponential (SE) function expressed as  $Kt^{\beta-1}\exp[-(t/\tau_0)^\beta]$ , which is derived from a time-dispersive rate equation for monomolecular reactions. Here,  $\tau_0$  is the effective recombination time and  $\beta$  is a dispersion parameter ( $0 < \beta < 1$ ). The fact that the PL decay  $I(t)$  fits  $Kt^{\beta-1}\exp[-(t/\tau_0)^\beta]$  for various values of  $G$  ( $\leq 2 \times 10^{19}$   $\text{cm}^{-3}\text{s}^{-1}$ ) and  $T$  can be considered to be a manifestation of a time-dispersive monomolecular reaction in the DP recombination, for the reason described in [19].

Morigaki [34] estimated  $\beta$  and  $\tau_0$  by fitting the LESR intensity decay obtained by Yan et al. [7] to the SE function for various  $G$ . In Fig. 7(a), the error bars show  $\beta$  vs.  $G$  obtained from the PL decay  $I(t)$  of Fig. 6 and the squares ( $\square$ ) show  $\beta$  vs.  $G$  obtained by Morigaki from the LESR intensity decay [34]. Similarly in Fig. 7(b), the error bars show  $\tau_0$  vs.  $G$  obtained from the PL decay and the squares ( $\square$ ) show  $\tau_0$  vs.  $G$  obtained from the LESR intensity decay [34].

We adopted the non-linear least square fit programme of *Origin 7J* and the non-linear regress of the statistic package of *Mathematica* ver. 4 to fit the data to  $Kt^{\beta-1}\exp[-(t/\tau_0)^\beta]$ . The lengths of the error bars indicate the extents of  $\beta$  and  $\tau_0$ , in which the non-linear least square fit keeps the value of chi-squared within 1.5 times its minimum value.

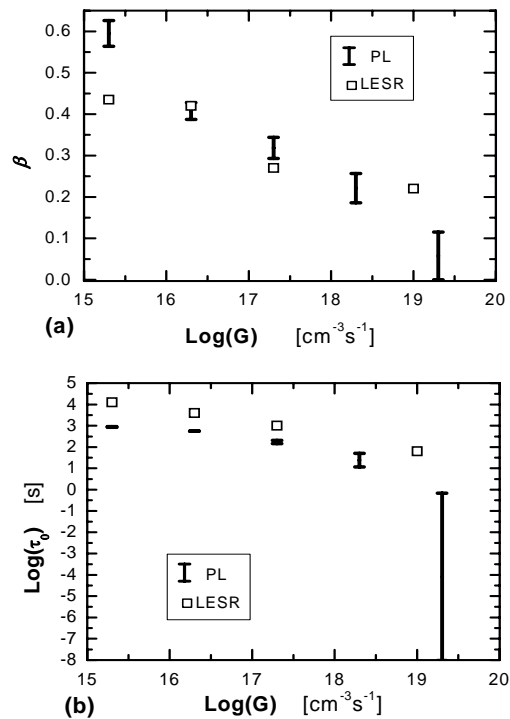


Fig. 7 (a)  $\beta$  vs.  $G$ , (b)  $\tau_0$  vs.  $G$ . The error bars from the PL decay of Fig. 6, squares ( $\square$ ) were obtained by Morigaki from the LESR decay [34].

In Figs. 7(a) and (b), we notice that  $\tau_0$  as well as  $\beta$  shows a very similar tendency in two different decay-measurements, i.e., the PL decay and the LESR intensity decay. The difference of an order in magnitude of  $\tau_0$  between the PL decay and the LESR decay is explained as follows.

Firstly, the measuring time  $t$  is very different between the two measurements; the PL decay was measured for  $t > 10^4$  s except for  $G = 2 \times 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$ , whereas the LESR decay was measured only up to  $t = 2 \times 10^3$  s [7]. Since  $\tau_0$  is relevant at long times, a short measuring time will lead to noticeable error. Actually, the PL decay at  $G = 2 \times 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$  was measured only to  $t \approx 2.7 \times 10^3$  s (Fig. 6), and thus  $\tau_0$  contains a considerable error, as shown by the longest error bar at  $G = 2 \times 10^{19} \text{ cm}^{-3} \text{ s}^{-1}$  in Fig. 7(b).

Secondly, the temperature is different between the two measurements. The PL decay was measured at 3.7 K, whereas the LESR decay was measured at 40 K, where the hop-up of electrons localized in band-tail states is no longer negligible; it enhances the DP recombination as well as the hopping transport [21,35]. In fact, at  $T = 40$  K,  $\tau_D$  is shortened and  $\eta_D$  is increased as described in Section 4, and furthermore  $n_D$  as well as the LESR density decreases to  $\sim 1/3$  of that at a low  $T$  [15,20]. Therefore, the temperature difference changes the kinetics of decay, resulting in the different values of  $\beta$  and  $\tau_0$  between the two decay phenomena.

Thirdly, the PL decay was excited at 2.33 eV, whereas the LESR decay was excited at 1.96 eV. This might have introduced an error of one order of magnitude in  $G$ , since  $G$  is proportional to the absorption coefficient, which changes widely in the range of these photon energies.

Finally,  $\tau_0$  is calculated according to the form  $A^{1/\beta}$  with one of parameters,  $A$ , coming from the non-linear least square fit, so that the error in  $\tau_0$  increases with decreasing  $\beta$ .

The integration of  $I(t)$  from  $t = 0$  to  $\infty$  is proportional to the metastable carrier density  $n_{\text{met}}$  at a continuous excitation rate  $G$  [19]. We plotted  $n_{\text{met}}$  ( $\times$ ) against  $G$  in Fig.

4, where the proportionality constant between the integral of  $I(t)$  and  $n_{\text{met}}$  is calculated by adjusting  $n_{\text{met}}$  to  $n_D$  at  $G = 2 \times 10^{16} \text{ cm}^{-3} \text{ s}^{-1}$ . Both  $n_{\text{met}}$  and  $n_D$  show sub-linear  $G$ -dependences ( $\propto G^{0.2}$ ), agreeing with the LESR densities [5-7]. These results support also that LESR reflects photocarriers localized in band-tail states, which subsequently recombine to give the long-lasting PL decay.

Moreover, as  $G$  decreases below  $\sim 10^{16} \text{ cm}^{-3} \text{ s}^{-1}$ ,  $n_{\text{met}}$  ( $\times$ ) as well as the LESR results deviates from the sub-linear dependence of  $G^{0.2}$ , with the deviation being larger for the defective a-Si:H (+) shown in Fig. 4. Actually, the PL decay curve of the defective film (plotted in half-tone) deviates more pronouncedly from the asymptotically converged curves at  $t \approx 10^3$  s (Fig. 6). Non-radiative recombination at the defect sites probably participates in shortening the fate of metastable carriers, since  $n_{\text{met}}$  becomes comparable with the defect density (Fig. 5) [19,35,36].

#### 4. Effect of electric field on geminate recombination and non-geminate (DP) recombination

The effect of a magnetic field of 0.9 T on the PL lifetime distribution was studied on a-Si:H [23] and a-As<sub>2</sub>Se<sub>3</sub> [16]. Application of the magnetic field to both materials weakened the DP recombination component and enhanced the triplet-exciton component, whereas it did not affect the singlet-exciton component. The quenching of the DP component was interpreted in terms of the paramagnetism of DP carriers. The enhancement of the triplet exciton component was explained by the Zeeman interaction due to  $S = 1$  for the triplet exciton; the singlet exciton has no Zeeman interaction because  $S = 0$ , thereby being unaffected by the magnetic field.

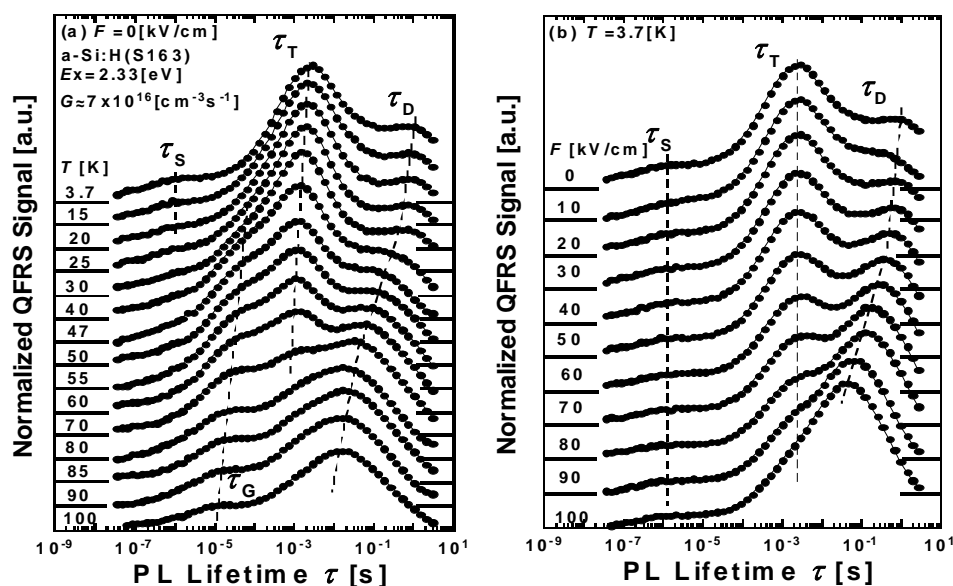


Fig. 8(a)  $T$ -evolved QFRS spectra of a-Si:H at  $F = 0$  kVcm $^{-1}$ . (b)  $F$ -evolved QFRS spectra of the same sample of (a) at  $T = 3.7$  K. PL was excited at  $E_X = 2.33$  eV and  $G \approx 7 \times 10^{16}$  cm $^{-3}$ s $^{-1}$  in both (a) and (b) [21].

The effect of an electric field  $F$  ( $\leq 100$  kVcm $^{-1}$ ) on the QFRS spectrum of the PL in a-Si:H was investigated in [21,22]. Figures 8(a) and (b) demonstrate the  $T$ -evolved QFRS spectra of the PL in a-Si:H at  $F = 0$  kVcm $^{-1}$  and the  $F$ -evolved spectra at  $T = 3.7$  K, respectively, both under the geminate condition ( $G \approx 7 \times 10^{16}$  cm $^{-3}$ s $^{-1}$ ) [21].

Roughly speaking, the effects of temperature and electric field resemble each other; increasing either  $T$  or  $F$  reduces the excitonic components, but enhances the DP component. However, a crucial difference between Figs. 8(a) and (b) is the appearance of a new lifetime ( $\tau_G$ ) component between  $\tau_S$  and  $\tau_T$  above  $T = 25$  K in Fig. 8(a). This has already been explained by the formation of geminate e-h pairs; as  $T$  rises above 25 K, excitation of thermal phonons prevents photogenerated e-h pairs from forming excitons, whereas non-excitonic, i.e., spin-free geminate pairs can be formed instead [15,20].

Since an electric field does not induce the phonon excitation, the electric field quenching of the excitonic or geminate component at low  $T$  has been explained in terms of the  $F$ -induced dissociation of excitons or geminate e-h pairs by various authors [3, 37-40].

In contrast to the excitonic or geminate component, however, we can see the shortening of the lifetime  $\tau_D$  as well as the enhancement of the DP component with increasing  $T$  (Fig. 8(a)) and with increasing  $F$  (Fig. 8(b)). The DP lifetime  $\tau_D$  is shortened by almost 2 orders of magnitude in the PL of undoped a-Si:H subjected to a strong electric field up to 100 kVcm $^{-1}$  at  $T = 3.7$  K.

The shortening of the lifetime  $\tau_D$  accompanied by the enhancement of the QE  $\eta_D$  with increasing  $T$  cannot be explained by the competition with non-radiative recombination, e.g. due to thermally-excited phonons. This temperature effect on the DP component is

interpreted in terms of increasing the number of recombination paths as well as the hopping diffusion, due to the hop-up of electrons localized in band-tail states by elevated  $T$  [35]. This is supported by the enhancement of  $\eta_D$  and shortening of  $\tau_D$  by superposing infrared (IR) light in the PL of a-Si:H; it enhanced not only the DP recombination but also photoconductivity (PC), i.e., the hopping transport of a-Si:H at low  $T$  [13,40].

In a strong electric field at  $T = 0$ , an electron can increase its energy with respect to the mobility edge by hopping over a distance against the electric field. This is analogous to an activation at a finite, or *effective* temperature  $T$ , and thus  $F$  plays a role similar to  $T$  for the hopping conduction [41]. The interplay between the  $T$ - and  $F$ -dependences of the lifetime  $\tau_D$  is interpreted on the basis of the *effective temperature* theory developed for the high-field hopping transport of charge carriers in disordered materials at low  $T$  [21,35,41].

The proportionality factor between  $T$ - and  $F$ -dependences of  $\tau_D$  is  $\sim 0.6$ , which is close to that obtained from those of the transport coefficients [21]. Our experimental results, therefore, prove that the DP recombination event is closely connected to the transport phenomena in a-Si:H as predicted by the theory based on the photocarriers localized in band-tail states [35].

## 5. Summary

The triple-peaked lifetime distribution obtained by wideband QFRS reveals that PL in a-Si:H at low  $T$  and low  $G$  originates from both excitonic recombination and DP recombination. The triple-peaked lifetime distribution has been universally observed in amorphous



chalcogenides as well as tetrahedrally-bonded amorphous semiconductors.

The steady-state carrier density of the DP component in the QFRS spectra agrees with the LESR density in the  $G$ - and  $T$ -dependences in a-Si:H. The residual PL decay observed up to  $t > 10^4$  s shows striking similarities to the LESR results in the  $G$ -dependences of the metastable carrier density and the two fitting parameters of the SE function, supporting the conclusion that the DP component and the LESR signal share common origins.

Application of an electric field to a-Si:H decreases the excitonic recombination by field-induced exciton dissociation, while it enhances the DP recombination. The latter is interpreted in terms of the *effective temperature* theory for the photocarriers localized in band-tail states.

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